Economics of Banking Lecture 9

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Shadow banking II

- A model of shadow banking
- Business cycles and financial intermediation
- Leverage cycles

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A model including all sectors

Two periods, t = 1, 2, two commodities. Agents:

(1) A *consumer* with W of good 1 and a utility function, the two goods are considered equal.

(2) A producer delivering good 2 at t = 2. Input N_1 of good 1 must be decided upon in t = 1. It can be revised at t = 2 to N_2 at a cost of $\frac{k}{2}(N_2 - N_1)^2$, production cost is c times output. No need for a loan.

Trade only at t = 2, and the consumer must store commodity 1 using one of the two financial agents:

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Financial agents

(3) A *bank* with two investment options:

- 1. payment of I at t = 1: if type G outcome L + I, if type B only L. All agents assume that the investment is G with a probability p.
- 2. payment of x and repayment

x + f(x) with probability q x with probability 1 - q.

This investment must be financed entirely by equity.

(4) A *trust fond* which can store the commodity – one unit in, one unit out.

Consumer puts W in bank or trustfund, takes it out as W_2 .

Producer adjusts to demand. Price is set to 1, so profit is

$$(1-c)W_2 - \frac{k}{2}(W_2 - N_1)^2.$$

 W_2 is random, so N_1 is taken as its mean value, expected profit is

$$(1-c)\mathsf{E}\widetilde{W}_2 - rac{k}{2}\mathsf{E}(\widetilde{W}_2 - \mathsf{E}\widetilde{W}_2)^2 = (1-c)\mathsf{E}\widetilde{W}_2 - rac{k}{2}\mathsf{Var}(\widetilde{W}_2).$$

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Bank offers security based on an investment portfolio:

Repayment: μL if portfolio is B, $\mu L + \lambda I$ if G.

Average return to consumer (and price of security) is $\mu L + p\lambda I$, bank gets rest, uses the cash payment for second investment

Consumer puts remainder $W - \mu L - \lambda p I$ into trust fund and takes it out at t = 2, so that W_2 has

► mean
$$p(W + (1 - p)\lambda I) + (1 - p)W - p\lambda I = W$$
,

► variance $p(1-p)\lambda^2 l^2$

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Regulation

Bank profit is

$$L + pl - l + qf(\mu L + \lambda pl - l).$$

increasing in μ and λ , without regulation set to 1 (leverage of bank's investment).

Regulation: Assume that regulator can set μ and λ so as to maximize total expected payoff of agents (= bank and producer)

$$L+pl-l+qf(\mu L+\lambda pl-l)+W(1-c)-rac{k}{2}p(1-p)\lambda^2l^2.$$

Optimal value of μ is 1. First order condition in λ is then

$$qf'(\lambda pl + L - l)pl - kp(1 - p)\lambda l^2 = 0$$

The optimal λ^* may be set indirectly by a limit on consumer share of investment. イロト イポト イヨト イヨ

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7 / 23

March 2023

Shadow banking

Now we allow the trust fund to become active: Buy a share in the portfolio (not allowed for consumers).

If price < 1, Bank will sell a share with probability 1 - p + pq (otherwise not interested)

The price will be $r = \frac{pq}{1-p+pq}$ (probability of getting money back)

Bank chooses λ' maximizing expected profit

$$(p\lambda + r\lambda')I + L - I + f((p\lambda + r\lambda')I + L - I) + (1 - \lambda - \lambda')I,$$

First order condition

$$rl + f'((p\lambda + r\lambda')l + L - l)rl - l = 0,$$

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Welfare conditions 1

Insert r and get

$$f'((p\lambda + r\lambda')I + L - I) = \frac{1-r}{r}$$

If $0 \leq \lambda' \leq 1 - \lambda$ then regulator's λ must lie between

$$\overline{\lambda} = \frac{\varphi\left(\frac{1-p}{pq}\right) + l - L}{pl} \quad \text{and} \quad \widehat{\lambda} = \frac{\varphi\left(\frac{1-p}{pq}\right) + l - L - rl}{(p-r)l}$$

(φ is the inverse of f')

Here $\overline{\lambda} > \widehat{\lambda}$. We conclude:

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Welfare conditions 2

- (I) If $\lambda \geq \overline{\lambda}$, then no shadow banking at all. If $\lambda \leq \widehat{\lambda}$, then bank sells $(1 \lambda)I$ to trust fund.
- (II) If $\hat{\lambda} < \lambda_1 < \lambda_2 < \overline{\lambda}$, then λ_2 is Pareto-better than λ_1 (tightening capital regulation is counterproductive).

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A dynamic model with credit and collateral

Economy over time, $t = 0, 1, \ldots$:

- one consumption good in each period
- capital good 'land' can be used as collateral and for production
- two types of agents:
 - (i) *entrepreneurs* own the land but have no endowment of consumption good
 - (ii) *lenders* with endowments of consumption good
- Production: one unit consumption good plus k units of land to yield y units of the consumption good in the next period.

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Dynamics in the model

At time t: Price of land is q_t .

Entrepreneur can obtain $q_{t+1}(1+r)^{-1}$ of the consumption good as a loan using land as collateral.

Then units of the consumption good, the entrepreneur needs $kq_{t+1}(1+r)^{-1}$ units of land.

The remaining $1 - kq_{t+1}(1+r)^{-1}$ can be rented out at a rate h_t , giving income $h_t[1 - kq_{t+1}(1+r)^{-1}]$.

Assume that rent is determined by $h_t = b - al_t$.

Fundamental equation

We then have the relation between land price in t and t + 1:

$$q_{t+1} + (y - (1 + r)) \frac{q_{t+1}}{1 + r} + h_t \left(1 - \frac{kq_{t+1}}{1 + r}\right) = q_t(1 + r).$$

Insert h_t , then q_t is a second-degree polynomial in q_{t+1} ,

$$q_t = \phi(q_{t+1}).$$

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Backward dynamics



A simple model of securities trading

Two periods, 0 and 1; one good, to be consumed or stored

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Infinitely many individuals i \in [0, 1].
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Individuals have one unit of the good AND an asset with payoff in the next period:



Individuals have subjective probability of success, uniformly distributed in [0, 1].

March 2023

15 / 23

Trade only

Individuals with small values of i sell their asset to individuals with larger i.

Equilibrium at price p of asset such that

$$\rho = i \cdot 1 + (1 - i) \frac{1}{4} \tag{1}$$

Market clearing occurs when

$$p \cdot i = 1 - i.$$

In our case we get i = 0.59, p = 0.69.

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Trade and loans

Optimistic individuals borrow goods and buy assets

Loans must be fully collateralized (by assets):

Since the asset pays only 1/4 in the case of a failure, borrowed amount y must satisfy

$$y-1=\frac{1+\frac{1}{4}y}{p},$$

Equilibrium conditions are (1) and:

$$p\cdot i=(1-i)\cdot 1+\frac{1}{4}$$

(buyers use their endowment plus the amount borrowed).

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Solution: i = 0.7, p = 0.78.

Loan to value ratio is 0.25/0.78 = 32%, and the haircut (percentage subtracted from the market value of the asset) is 0.53/0.78 = 70%.

Leverage, value of assets divided by own capital invested, is

$$\frac{0.78}{0.78 - 0.25} = 1.47$$

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One more period

Change the setup to three periods:



Loans are *repo* contract: Lender buys the asset from the borrower, who must buy it back after one period.

Finding equilibrium I

At t = 1: In the state D marginal individual is i_1 . At t = 0: i_0 . The counterpart of (1) is

$$p_D = i_1 1 + (1 - i_1) \frac{1}{4},$$

and market clearing at state D is

$$rac{i_1}{i_0} p_D = rac{i_1}{i_0} (i_0 - i_1) + rac{1}{4}.$$

To the left: Only the individuals up to $i \leq i_0$ in the market, each holds $\frac{1}{i_0}$. To the right: Goods for sale with individuals in $[i_1, i_0]$, plus what can be borrowed.

Rewrite market clearing as

$$i_0 = \frac{4}{5}i_1(1+p_D).$$

Finding equilibrium II

We must also find i_0 and p_0 . We have

$$i_0 p_0 = (1 - i_0) + p_D,$$
 (2)

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21 / 23

(amount of goods transferred to sellers t = 0 equals amount of goods that the buyers own plus what they can borrow) Determining the marginal individual i_0 : An asset gives $1 - p_D$ in state U and 0 in D, against a downpayment of $p_0 - p_D$, so that

$$i_0 \frac{1 - p_D}{p_0 - p_D}$$

Or: i_0 may keep the good to t = 1, which with probability i_0 keeps its value at U and with probability $(1 - i_0)$ can be leveraged purchase of asset at t = 2. 1

$$i_0 rac{1-rac{1}{4}}{p_D-rac{1}{4}} = rac{i_0}{i_1},$$

Equilibrium results

Solving the system of 4 equations gives

$$i_1 = 0.638, \quad p_D = 0.729,$$

 $i_0 = 0.882, \quad p_0 = 0.959.$

Leverage at t = 0:

$$\frac{0.959}{0.959 - 0.729} = 4.16$$

At t = 1 (in D) changed to

$$\frac{0.729}{0.729 - 0.25} = 1.522$$

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