

# Economics of Banking

## Lecture 14

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# Diamond-Dybvig again

Investment project  $I$  with payoff  $R > 1$  per unit.

Individuals subject to liquidity shock at date  $t = 1$  with probability  $\pi$ .

Optimal arrangement: Deposit contract.

Bank delivers either  $c_1^0$  at  $t = 1$  or  $c_2^0$  at  $t = 2$ , such that

$$\max_{c_1, c_2, I} \pi u(c_1) + (1 - \pi)u(c_2)$$

subject to constraints

$$\begin{aligned} \pi c_1 &= 1 - I, \\ (1 - \pi)c_2 &= RI. \end{aligned}$$

## Sunspot equilibria

Suppose that *patient* depositors become afraid that bank will not pay at  $t = 2$ :

Then they they will prefer  $c_1$  at  $t = 1$  to nothing at  $t = 2$ .

*Bank run*: Bank cannot satisfy its obligations and is bankrupt.

The initial beliefs of turned out to be justified!

(Extended model: Add a mechanism producing signal  $s \in \{0, 1\}$ .)

If the depositors believe that  $s = 1 \Rightarrow c_2 = 0$ , then running the bank is optimal choice, and:

Beliefs sustained: This is an example of a *sunspot equilibrium*.)

# How can bank runs be prevented?

We shall be concerned with several proposals for preventing than bank runs happen:

(1) **Suspension of payment:** Bank declares that it will pay out only the amount corresponding to  $c_1$  times number of impatient depositors.

Effect: Patient depositors can see that the bank will survive to  $t = 2$ .

Problem: The share  $\pi$  of impatient must be observed with high precision.

Works only in theory. Points to insurance of deposits (to be treated later).

# Deposit certificates instead of deposits

## (2) Deposit certificates

Certificates with dividend payment  $d$  at  $t = 1$ , giving  $R(1 - d)$  at  $t = 2$ .

Impatient individuals sell the certificate at price  $p$  and gets

$$c_1 = d + p,$$

Patient individuals buy  $\frac{d}{p}$  and get

$$c_2 = \left(1 + \frac{d}{p}\right) R(1 - d).$$

## Finding the optimal dividend

The price  $p$  is found by supply=demand,

$$\pi = (1 - \pi) \frac{d}{p} \text{ or } p = \frac{1 - \pi}{\pi} d,$$

so

$$c_1 = \frac{d}{\pi}, \quad c_2 = \frac{R(1 - d)}{1 - \pi}.$$

Dividend payment can be specified to achieve optimum.

Problem: Depends on the correct setting of  $d$ .

Does away with traditional banking (shareholders instead of depositors).

# Narrow banking

## (3) **Narrow banking**

Banks taking deposits should invest only in safe securities (sold at full value at any time). so that the bank runs cannot occur.

In the context of the D-D model: The constraints are

$$c_1 \leq 1 - l$$

$$c_2 \leq Rl,$$

Maximizing expected utility here is inferior to the D-D solution, preventing banking as we understood it so far.

Too simple formalization – narrow banking is about separating the activities of banks.



# Liquidity risk

Liquidity can be considered as an inventory problem:

Assume: Bank gets  $r_L$  on loans but must pay penalty rate  $r_p$  if reserves  $R$  too small.

Depositors' demand  $\tilde{x}$  has probability distribution function  $F(x)$  and density  $f(x)$ .

Expected profit

$$\pi(R) = (D - R)r_L + Rr - r_p \int_R^\infty (x - R)f(x) dx.$$

# Optimal reserves

First order conditions for a maximum:

$$-r_L + r + r_p \int_R^\infty f(x) dx = 0$$

and since  $\int_R^\infty f(x) dx = 1 - F(x)$ ,

$$1 - F(R) = P\{\tilde{x} \geq R\} = \frac{r_L - r}{r_p}.$$

Model not realistic: Suppose that  $r_L - r = 4\%$  and  $r_p = 20\%$ .

Then the probability of being short of cash is  $1/5$ .

# Basel III

Liquidity risk was **not** considered in Basel I and II.

Basel III introduces:

- ▶ a *liquidity coverage ratio*: High quality assets must cover one month net cash outflow.
- ▶ a ratio between long-term assets, suitably risk weighted, and *net stable funding* (deposits, long-term loans and equity).

Criticism: financial supervisors may not be the right institutions for dealing with questions of liquidity (better to use lenders of last resort).

## Many banks with different depositors

Now there are  $n$ , banks, and bank  $j$  has depositors with probability  $\pi_j$  of being impatient. Average probability is  $\bar{\pi}$ .

Bank  $j$  proposes deposit contract  $(c_1^j, c_2^j)$ .

In the social optimum the contracts should maximize

$$\frac{1}{n} \sum_{j=1}^n [\pi_j u(c_1^j) + (1 - \pi_j) u(c_2^j)]$$

under the constraints

$$\frac{1}{n} \sum_{j=1}^n \pi_j c_1^j = 1 - I,$$

$$\frac{1}{n} \sum_{j=1}^n (1 - \pi_j) c_2^j = RI,$$

$$0 \leq I \leq 1.$$

# Properties of optimum

By concavity of  $u$  (risk aversion):

All individuals get the same contract  $(c_1^*, c_2^*)$ , independent of bank.

If  $l^*$  is the investment supporting the contract, then at  $t = 1$  we have:

$$\text{Average need for liquidity} = \frac{n_1}{n} \sum_{j:\pi_j > \bar{\pi}} \pi_j c_1^* - \frac{n_1}{n} (1 - l^*),$$

$$\text{Average surplus of liquidity} = \frac{n_2}{n} (1 - l^*) - \frac{1}{n} \sum_{j:\pi_j \leq \bar{\pi}} \pi_j c_1^*,$$

with  $n_1$  and  $n_2 = n - n_1$  are the numbers of banks with deficit resp. surplus.

## The interbank rate

At  $t = 2$ , the loans are paid back with an interbank interest rate  $r$ .

Surplus (at  $t = 1$ ) banks can use this when paying back at  $t = 2$ :

$$(1 + r)(1 - I^* - \pi_k c_1^*) = (1 - \pi_k) c_2^* - RI^*,$$

and borrowers can use the surplus at  $t = 2$  to pay back debt,

$$(1 + r)[\pi_j c_1^* - (1 - I^*)] = RI^* - (1 - \pi_j) c_2^*,$$

Insert  $1 - I^* = \bar{\pi} c_1^*$  and  $RI^* = (1 - \bar{\pi}) c_2^*$ :

$$(1 + r)(\bar{\pi} - \pi_j) c_1^* = [(1 - \pi_j) - (1 - \bar{\pi})] c_2^* = (\bar{\pi} - \pi_j) c_2^*,$$

so that  $(1 + r) = \frac{c_2^*}{c_1^*}$  or

$$(1 + r) = \left( \frac{\bar{\pi}}{1 - \bar{\pi}} \right) \left( \frac{I^*}{1 - I^*} \right) R.$$

# Interbank market with uncertainty

As before, probability of impatience differ, here: either  $\pi_h$  or  $\pi_l$ ,

As always, investment can be liquidated at  $t = 1$  at a value  $L < 1$  per unit.

**New feature:** The investment is subject to uncertainty:

Outcome is  $R$  with some probability  $u$ , 0 otherwise, where

$$u = \begin{cases} u_S & u_S > u_r \\ u_l & \end{cases}$$

The probability is revealed to the relevant bank only at  $t = 1$ ;

# Full information

Size of deposit withdrawals  $j \in \{h, l\}$  and quality of investment  $i \in \{r, s\}$  can be observed by all banks at  $t = 1$ .

Then there will be different interest rates,  $r_s$  and  $r_r$ , for to the two types of borrowers.

Lenders get the expected payoff  $u_s(1 + r_s)$  from  $s$ -borrowers and  $u_r(1 + r_r)$  from  $r$ -borrowers, so

$$u_s(1 + r_s) = u_r(1 + r_r).$$



# Equilibrium

A bank with a large  $\pi_h$  needs a loan of size  $\pi_h c_1 - (1 - I^*)$ .

The rates  $r_s$  and  $r_r$  can be found from the condition to be satisfied at  $t = 2$ :

$$\begin{aligned}(1 + r_i)(\pi_h c_1 - (1 - I^*)) &= u_i R I^* - (1 - \pi_h) c_2, \\ (1 + r_i)[(1 - I^*) - \pi_l c_1] &= (1 - \pi_l) c_2 - u_i R I^*\end{aligned}$$

$i = s, r$ , and the average rate (given the proportion of safe and risky projects) is

$$\rho_0 = \frac{\hat{\pi}}{1 - \hat{\pi}} \frac{I^*}{1 - I^*} \hat{u} R$$

(much as before)

## Asymmetric information

If lenders cannot observe whether borrower is  $s$  or  $r$ , then there is only one rate  $\rho_1$ .

(1) Let  $u'$  be average probability. If  $u'\rho_1 < 1$ , there will be no lenders.

(2) If both  $r$  and  $s$  banks are borrowing, then  $u' = \hat{u}$ , and the repayment rate  $\rho_1$  is found as in the B-G model

$$\rho_1 = \frac{\hat{\pi}}{1 - \hat{\pi}} \frac{I^*}{1 - I^*} \hat{u}R.$$

(3) In this case, it expected profit for a borrower is

$$u(RI^* - (1 - \pi_h)c_2 - \rho_1(\pi_h c_1 - (1 - I^*))) - (1 - I^*).$$

and *not* using the market, it is

$$u\left(R(I^* - \frac{1}{L}(\pi_h c_1 - (1 - I^*))) - (1 - \pi_h)c_2\right) - \pi_h c_1$$

# The drying out of the interbank market

Rewriting the two equations as

$$u(RI^* - (1 - \pi_h)c_2) - [u\rho_1\pi_h c_1 + (1 - u\rho_1)(1 - I^*)]$$

and

$$u(RI^* - (1 - \pi_h)c_2) - \left[ \left( 1 + \frac{uR}{L} \right) \pi_h c_1 - \frac{uR}{L} (1 - I^*) \right].$$

If  $u_s \approx 1$  and  $u_s$  small so that  $\rho_1$  is large (remember,  $u'\rho_1 > 1$ ), then *not* borrowing is better for s-borrowers if  $\frac{uR}{L}$  is close to 1.

Consequence: *Adverse selection*, only bad borrowers, lenders may stay away.