# Economics of Banking <br> Lecture 11 

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## Table of contents

## Diverse topics

- Cryptocurrencies
- Islamic Banking


## Competition and pricing

- Banking under perfect competition
- The monopolistic Bank
- Oligopolistic banks


## BitCoin

First electronic means of payments without intermediation

Introduced by Nakamoto 2008, now other cryptocurrencies have been developed

Fundamental problem for means of payment:

How can it be guaranteed that the money is used only once?
BitCoin: Internet community check that money is used correctly

## Blockchain

Transactions are recorded in special data structure:


A new block of transactions can be checked by any individual (a "miner"), showing that it is ok

To perform this, the miner must solve a complicated (time and energy consuming) problem (find the inverse of a specific cryptographic function)

Blockchain technology is interesting also for banks (and central banks)

## Pros and Cons of BitCoin

No (or almost no) cost of money transfers

Decentralized system (not subject to monetary policy)

But:

BicCoin has limited capacity

Transfer is slow (up to 10 minutes before a transfer is confirmed)

The mining process is energy-intensive

## Negative interest rates

Interest rates have been moving downwards for decades

Currently many interest rates are negative

Combined with small annual growth rates

What are the implications for:

- Macroeconomic stability (to be dealt with in Macro)
- Monetary policy (to be considered in Monetary Economics)
- Financial intermediation?


## Islamic Banks

Banking without interest payments:
Basic principles:
(1) risk-sharing: symmetric distribution of risk and return,
(2) materiality: linkage to real activity,
(3) no exploitation
(4) no financing of prohibited activities

Main forms of financing:

- Participatory form: Bank is business partner (more or less active)
- Non-participatory form (trade-based): Bank initiates investment and allows the investor buys it back

Islamic banks quite succesful ( $70 \%$ of financial assets in selected countries)

## Perfect competition

Given: Ioan (interest) rate $r_{L}$, the deposit rate $r_{D}$, interbank rate $r$
Bank chooses loans $L$ and deposits $D$ to maximize profits

$$
\pi(D, L)=r_{L} L+r C-r_{D} D-c(D, L)
$$

(with $C$ net position in the interbank market, $c(D, L)$ managing cost)

If $0<\alpha<1$ of deposits are kept as reserve, then $C=(1-\alpha) D-L$, and

$$
\pi(D, L)=\left(r_{L}-r\right) L+\left((1-\alpha) r-r_{D}\right) D-c(D, L)
$$

First order conditions are

$$
\frac{\partial \pi}{\partial L}=r_{L}-r-c_{L}^{\prime}=0, \quad \frac{\partial \pi}{\partial D}=(1-\alpha) r-r_{D}-c_{D}^{\prime}=0
$$

## Market equilibrium

How is $r$ determined?

There are $n$ banks, demand for loans comes from investment function $I\left(r_{L}\right)$, so that

$$
I\left(r_{L}\right)=\sum_{j=1}^{n} L_{j}\left(r_{L}, r_{D}, r\right)
$$

Household saving depends on $r_{D}$, so

$$
S\left(r_{D}\right)=B+\sum_{j=1}^{n} D_{j}\left(r_{L}, r_{D}, r\right)
$$

where $B$ is bond issue (by government).
Finally, the interbank marketmust be balanced:

$$
\sum_{j=1}^{n} L_{j}\left(r_{L}, r_{D}, r\right)=(1-\alpha) \sum_{j=1}^{n} D_{j}\left(r_{L}, r_{D}, r\right)
$$

## A Digression: The money multiplier

Simple version: Bond changed by $\triangle B$, then deposits change by the same amount.
Then banks can expand credits by $(1-\alpha) \triangle B$, again changing deposits, and summing all:

$$
\triangle D=\triangle B\left(1+(1-\alpha)+(1-\alpha)^{2}+\cdots\right)=\frac{1}{\alpha} \triangle B
$$

More sophisticated version, using our model: Inserting the first two equations in the last one:

$$
S\left(r(1-\alpha)-c_{D}^{\prime}\right)-\frac{l\left(r+c_{L}^{\prime}\right)}{1-\alpha}-B=0
$$

Determines $r$ as an implicit function of $B$.

## Open market policies

Use implicit function theorem:

$$
\frac{d r}{d B}=\frac{1}{(1-\alpha) S^{\prime}-\frac{I^{\prime}}{1-\alpha}}
$$

Then

$$
\frac{\partial D}{\partial B}=(1-\alpha) S^{\prime} \frac{d r}{d B}-1=\frac{(1-\alpha) S^{\prime}}{(1-\alpha) S^{\prime}-\frac{I^{\prime}}{1-\alpha}}-1=\frac{1}{\frac{(1-\alpha)^{2} S^{\prime}}{I^{\prime}}-1}
$$

If $S^{\prime}>0, I^{\prime}<0$, then

$$
\frac{\partial D}{\partial B}<0
$$

as expected, but

$$
\left|\frac{\partial D}{\partial B}\right|<1
$$

Money multiplier is small!

## The Monti-Klein model

Bank maximizes profits

$$
\pi(D, L)=\left(r_{L}(L)-r\right) L+\left((1-\alpha) r-r_{D}(D)\right) D-c(D, L)
$$

First order conditions are

$$
\begin{aligned}
& \frac{\partial \pi}{\partial L}=r_{L}^{\prime} L+r_{L}-r-c_{L}^{\prime}=0 \\
& \frac{\partial \pi}{\partial D}=-r_{D}^{\prime} D+(1-\alpha) r-r_{D}-c_{D}^{\prime}=0
\end{aligned}
$$

Can be reformulated in several ways:

## Lerner index

(1.) 1st order conditions using Lerner indices:

$$
\frac{r_{L}-\left(r+c_{L}^{\prime}\right)}{r_{L}}=-\frac{r_{L}^{\prime L}}{r_{L}}=\frac{1}{-\frac{r_{L}}{r_{L}^{\prime}}}=\frac{1}{\varepsilon_{L}},
$$

where

$$
\varepsilon_{L}=-\frac{L^{\prime}}{\frac{L}{r_{L}}}
$$

Similarly for the deposit rate

$$
\begin{equation*}
\frac{r(1-\alpha)-r_{D}-c_{D}^{\prime}}{r_{D}}=\frac{1}{\varepsilon_{D}}, \tag{1}
\end{equation*}
$$

with $\varepsilon_{D}=r_{D} D^{\prime} / D$.

## Amoroso-Robinson

(2.). 1st order condition expressed using the Amoroso-Robinson formula:

For the loan rate:

$$
r_{L}=\frac{r+c_{L}^{\prime}}{1-\frac{1}{\varepsilon_{L}}} .
$$

and for the deposit rate:

$$
r_{D}=\frac{(1-\alpha) r-c_{D}^{\prime}}{1+\frac{1}{\varepsilon_{D}}}
$$

## Application: Taxing banks

Proposed as a way of making banks more secure (after the crisis 2007-8) Suppose that a tax is collected as a fixed percentage $t$ of the loans $L$. Then profits are

$$
\pi(D, L)=\left(r_{L}(L)-(r+t)\right) L+\left((1-\alpha) r-r_{D}(D)\right) D-c(D, L)
$$

and 1st order condition wrt $L$ become

$$
\frac{r_{L}-\left(r+t+c_{L}^{\prime}\right)}{r_{L}}=\frac{1}{\varepsilon_{L}},
$$

1st order condition wrt $r_{D}$ is as before.
The Lerner index is unchanged if $\varepsilon_{L}$ is constant: The tax is shifted to the borrowers.

Depositors are unaffected if $c_{D}^{\prime}$ is independent of $L(c(D ; L)$ separable in $D$ and $L$ )

## Oligopoly

Suppose that there are not one but a few (namely $N$ ) banks. Banks choose quantities (Cournot oligopoly) to maximize

$$
\pi_{i}(D, L)=\left(r_{L}(L)-r\right) L_{i}+\left((1-\alpha) r-r_{D}(D)\right) D_{i}-c\left(D_{i}, L_{i}\right)
$$

with $L=\sum_{i=1}^{N} L_{i}, D=\sum_{i=1}^{N} D_{i}$.
First order conditions:

$$
\begin{aligned}
& \frac{\partial \pi}{\partial L}=r_{L}^{\prime} L_{i}+r_{L}-r-c_{L}^{\prime}=0 \\
& \frac{\partial \pi}{\partial D}=-r_{D}^{\prime} D_{i}+(1-\alpha) r-r_{D}-c_{D}^{\prime}=0
\end{aligned}
$$

Symmetric case: Lerner indexes are

$$
\frac{r_{L}-\left(r+c_{L}^{\prime}\right)}{r_{L}}=\frac{1}{N \varepsilon_{L}}, \quad \frac{r(1-\alpha)-r_{D}-c_{D}^{\prime}}{r_{D}}=\frac{1}{N \varepsilon_{D}}
$$

